

RESEARCH ARTICLE

HEAVY IONS REACTIONS WITH TWO NUCLEON TRANSFER.

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Manuscript Info	Abstract
Manuscript History	$The^{64}Ni(^{16}O.^{14}C)^{66}Zn$ two proton pickup reactions has been studied .at
Received: 03 December 2016 Final Accepted: 06 January 2017 Published: February 2017	56Mev of ¹⁶ O projectile energy, the differential cross section have been evaluated in the frame work of the exact finite-range distorted wave Born approximation using folding model for the real part of optical nuclear potential. The calculated angular distributions are fitted with the experimental data.
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Introduction:-

The two nucleon transfer reactions have been taken on great importance ,because they are very sensitive to nuclear spectroscopy, heavy ion transfer reactions are valuable tools for getting precise spectroscopic information's [1, 2]. The right framework in which the reaction be treated is Distorted Wave Born Approximation (DWBA) ,or Coupled Channel Born approximation (CCBA) methods [3,4] with inclusion the nuclear recoil. Two nucleon transfer reactions induced by heavy ions had been widely considered [5] by using DWBA with nucleon –nucleon interactions which include both attraction and repulsion.

In the present study ,the differential cross section of heavy ion reaction with two proton pickup reaction have been calculated in The 64 Ni(16 O, 14 C) 66 Zn reaction at 56 Mev of 16O projectile energy, analysis concentrated on g.s. ,first 2⁺ ,first 3⁻ excited levels. The 64 Ni(16 O, 14 C) 66 Zn are studied by Mermaz [7] by using coupled channel Born approximations and distorted wave born approximation calculations and he conclude that the relative intensities among various states are better reproduced by CCBA than DWBA calculations , the present work is like Memaz study using DWBA but the optical potential model was taken to be folded for the real part of optical potential , the phenomenological optical potential are often successfully used to describe the heavy ion elastic scattering data ,the use of folding model allows us to predict potential and eliminate the ambiguities which appear with the phenomenological potential. Folding model gives better interpretation as a basic physical ingredients the nuclear densities folded with a nuclear interaction in correct way. The calculated angular distributions are fitted with the experimental data.

The differential cross section of heavy ion reaction with nucleon Transfer:

The differential cross section of heavy-ion reaction with two nucleons pickup

A(b,a)B where A is the target B is the residual nucleus ,b is the projectile A=B+c , and a = b + c , and the c is the two – proton cluster, is given by the expression:

 $\frac{d\sigma}{d\Omega} = \frac{m_{aB} m_{bA}}{(2\pi\hbar^2)^2} \frac{K_{aB}}{K_{bA}} \frac{1}{2S_b + 1} \sum_{LM} \left| T_{fi} \right|^2$

Where m_{bB} , m_{bA} are the reduced masses of pair (a, B), (b, A) respectively, and the matrix element T_{fi} represent the DWBA transition amplitude that has the form :

$$T_{fi} = \sum_{L_{cB} L_{cb} N_{cB} N_{cb}} B_{cB} \beta_{LM}$$

Where:

$$\beta_{LM} = \frac{(-1)^{L}}{\sqrt{2L+1}} \int dr_{bA} dr_{aB} X^{*} (r_{bA}) f_{LM} (\boldsymbol{r}_{cb}, \boldsymbol{r}_{cB})$$

$$f_{LM} = \sum_{A\bar{A}} (-1)^{L_{cB} + \bar{A}} \{ L_{cB} \Lambda L_{cb} | LM > \Phi_{A}^{*} (r_{cB}) V(\boldsymbol{r}_{cb}) \Phi_{\bar{A}} (\boldsymbol{r}_{cb})$$

$$B_{cB} = i^{L} \sum_{L_{c}} (\frac{2J_{a} + 1}{2L_{c} + 1})^{\frac{3}{2}} (-1)^{L_{cB} + L_{c} - J_{B}} U(I_{B} L_{cB} J_{a} L_{cb}; L_{c} L) A_{cB}^{*} A_{cb}$$

The dependence on kinematics and the reaction mechanism is contained in the factor β_{LM} , where f_{LM} (r_{cB} , r_{cB}) is the finite-range form factor. The spectroscopic dependence lies in the factor B_{cB} , and the two spectroscopic amplitude A_{cB} , A_{cb} contained therein.and V(r) is nuclear optical model potential in form of Wood-saxon, this form is given as :

$$V(r) = \frac{-V_0}{1 + \exp\{\frac{r - R_V}{a_v}\}} + \frac{-W_0}{1 + \exp\{\frac{r - R_w}{a_w}\}}$$

Where , the parameters V_0 , R_v and a_v , are the strength ,radius and diffuseness of the real potential ,while the parameters W_0 , R_w and a_w , are the strength ,radius and diffuseness of the imaginary part which are determined by fitting scattering reaction of the corresponding interaction of two heavy ions.

Numerical calculations and result and discussion and conclusion:-

The differential cross section has been numerically carried out for ${}^{64}\text{Ni}({}^{16}\text{O},{}^{14}\text{C}){}^{66}\text{Zn}$ reaction at 56Mev, in the frame work of the exact finite-range distorted wave Born approximation and the real double –folded potential used in an optical model analysis of elastic scattering data. The potentials were calculated by convoluting the M3Y effective nucleon – nucleon interaction[8], the necessary parameters of the optical potential are shown in table (1). here the results obtained for the differential cross section are shown in figure(1), figure(2) and figure(3).

Tuble (1) • Optical potential parameters used in <i>D</i> (<i>D</i>) • D) • enclutations							
Reaction	E _{lab}	\mathbf{W}_0	a_{w}	R _w	r _c	Ref.	
	(Mev)	(Mev)					
¹⁶ O+ ⁶⁴ Ni	56Mev	20	0.283	1.311	1.25	7	

Table (1): Optical potential parameters used in DWBA calculations



Figure 1:- The differential cross section ⁶⁴Ni(¹⁶O,¹⁴C)⁶⁶Zn reaction at 56 Mev incident energy leading to ⁶⁶Zn ground state .The solid curve is the present calculation and the dots are the experiment data taken from refernce (9).



 Θ_{cm} . **Figure2:**- The differential cross section ⁶⁴Ni(¹⁶O,¹⁴C)⁶⁶Zn reaction at 56 Mev incident energy leading to 66Zn at 1.040 Mev 2⁺ state .The solidcurve is the present calculation and the dots are the experiment data taken from reference (9)



Figure3:- The differential cross section 64Ni(16O,14C)66Zn reaction at 56 Mev incident energy leading to 66Zn at 2.830 Mev 3⁻ state. The solid curve is the present calculation and the dots are the experiment data taken from reference (9).

The shape of all angular distributions are in a good agreement with the experimantal data except that the angular distribution for transition 2⁺ states, it seem to be several degrees forward of the DWBA curve. In conclusion in this study despite the better shape of angular distributions with a little difference in the shape of angular distributions clalculated by DWBA using the double-folding model for the real part of optical potential and the previous calculations without using the folded model ,the CCBA calculations (8) which include multiple processes are more suitable than DWBA they give better a greement with experimantal data , and the double-folding potential are found to be appropriate to reproduce the cross-section and capable of producing realistic prediction of the angular distribution.

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