Effectiveness of Mathematics in the Electoral System: an

2 Analysis

3 Abstract:

- 4 Mathematics studies numbers and quantities, space, structure, patterns and mathematics
- 5 involves quantititive calculation and logical reasoning to explore pettens, formulate ideas and
- 6 it establish truth through deduction. mathematics is important in the fields namely
- 7 engeneering, science, medicine, and finance. Electoral System is used in politics to elect
- 8 government and it is a set of rules used to determine the outcomes of an election. Generally,
- 9 the common categorisations of electoral system are single winner vs. multi winner system,
- proportional representation vs. winner take all systems vs. mixed systems. The aim of the
- present study is to analyse the effectiveness of Mathematics in the electoral system.

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key words:

Electoral system, Mathematics, election, voting system.

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Introduction:

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- 18 Mathematics plays a key rule in Electoral System. Mathematics helps in forming electoral
- method, analysis and can predict the results. electoral systems can be classified into three
- 20 main families manely majoritarian, proportional and mixed. The key features of electoral
- 21 system are electoral formula, district magnitude, ballot structure, electoral thresholds, other
- procedural features, etc.
- 23 Mathematics plays a vital role in the analysis, designs and evaluation of electoral system. It is
- 24 important in the electoral system because it provides the theoretical foundations as well as
- 25 practical tools needed to design, analyze and protect fair elections. mathematical principles
- are important for auditing elections and protecting scencitive data.

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Objectives:

- To understand the importance of mathematics in voting system.
- To analyze the effectiveness of mathematics in the electoral systems

31 **Methodology:**

- 32 The current literature review related to mathematics and the Electoral System. The
- descriptive method has been applied to conduct the present study. Data has been collected
- 34 from secondary scurces namely books, articles, research paper and other existing literature.

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What is mathematics:

- 37 Mathematics is the study of number, patterns, shapes and logical reasonings. It is the most
- 38 important fields in human knowledge. From the beginning of civilization mathematics are
- 39 used to count things, calculate time, measure land etc. Today, mathematics has grown into a
- 40 very vast subject, it helps to know the real world and abstract ideas. Mathematics has so
- 41 many branches like geometry, algebra, arithmetic, trigonometry, probability etc. In short,
- 42 mathematics is more than numbers . It helps to sharpness the mind, increase logical ability ,
- devlope reasoning and that is why mathematics is called the "queen of all science".

44 Relationship Between Electoral System and Mathematics in

45 **Contemporary Areas:**

- 46 The study of elections is not only a part of politics but also highly connected with
- 47 Mathematics. Now a days Mathematics is used like a tool to make election transparent, fair
- and logical. The relationship between Mathematics and electoral system is very important
- because it helps to understand voting methods, predict outcomes and reduce injustices.

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• Mathematics in Design, Analysis and Evaluation of Electoral System:

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55 56 Using Mathematics is very important in design, analysis and evaluation of electoral systems. Different countries use different systems of voting. Each of the system based on Mathematics to count votes and declare results . With the help of Mathematics it is easy to explain how the system work and what result it can produce.

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60 61 Mathematics is also used in prediction and analysis. Part of Mathematics like Statistical models and Probability help media and researchers to predict the results even before the counting the votes or conduct the election. Also survey, opinion polls etc. give a very close idea that where people are more interested to give their valuable vote.

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- Evaluation in electoral system means determining the good and bad sides of the system. Mathematics helps to inquiry questions like
 - Do all parties get seats according to their votes?
 - Is the system fair to majority of people?
 - Can the system gives trusted results?

By using statistics, data analysis and computer models, Mathematics helps to conclude the system is fair and useful or not.

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Designing Different Voting Methods:

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Mathematics is used in designing different voting methods. Different countries use different voting methods.

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First-Past-the-Post (FPTP): India, UK use this method in elections. In this method, the candidate who gets the highest votes wins, no matter whether that candidate has received votes above the half. FPTP method is very simple to design and understand, however, candidates can win without receiving more than half of the votes.

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Proportional Representation (PR): Germany and other European countries use this method. In this method, seats are given to political parties in according to the amount of votes received. Mathematics is applied in the system of dividing the seats to be distributed by either the Quota method of the Divisor method.

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Ranked- Choice Voting (RCV): In this method of voting, the choice of the candidate is placed on a chosen list and are ordered for preference from first to last and the candidate is voted either to stand or be removed. When no candidate gets a majority, the candidate with the fewest votes is eliminated, and their votes are reassigned to the remaining candidates.

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Analysis Gerrymandering:

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Gerrymandering means drawing the boundaries of voter areas. It helps to prevent unfair way to give more advantage to one party. Mathematics is very useful in analysing and learning gerrymandering.

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Using Geometry: Mathematics is used to determine the shape of a district. If a district has a very unusual shape, it may be a sign of gerrymandering. A fair district usually has a simple and compact shape.

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i.e, more compact = more fair.

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Using Statistics: Statistical methods are used to compare votes and seats. Vote seat compassion, efficiency gap, mead-median test, simulation method are the main parts in Statistical methods.

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Using Graph Theory: Graph theory is mainly used to show the map for various district. It helps to connect populations.

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Predicting Voter Behaviour and Outcomes:

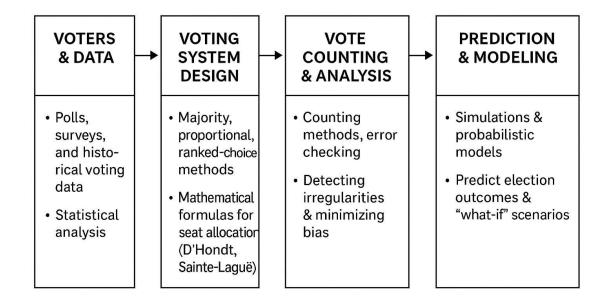
With the help of Mathematics researcher, media can predict the election results even before the counting. It includes historical data, surveys and mathematical models.

- Opinion Polls and Surveys: Opinion poll is the fast method to know what people thinking about upcoming election. In this method research ask a small group of people about their choice of voting and it shows which party might win. Survey is slow method. It refers collected information from people. Government can conduct surveys to know how many people are satisfied with education, healthcare or the other schems provided by the government.
- **Predictive Models:** Regression analysis, machine learning and Bayesian statistics are the main techniques in predictive models. It helps to predict results based on various factors like economy, candidate popularity etc. If economic growth is low, establishment is low then votes may shift against the ruling party.
- **Simulation of Electoral System:** Simulation means an experiment to see how something will work in real life. In election simulation of electoral system is used to predict results, test voting methods before the real election conduct. Collect dada, build a model, test with different voting methods, compare results, make analysis are the major parts of this method.

• Principles of Mathematics in Voting System:

- Mathematics plays a main part in presenting fair and effective voting system. Counting Methods, fairness, representation and probability are the main principals in voting system.
 - **Majority Rule:** It is the simplest principal that says the candidate more than half of the votes will win. Mathematics assure that the counting process is correct and transparent.
 - Ranking and Preferences Voting: In this methods voters rank their candidates in order of their preferences. The Instant Runoff Voting (IRV) or Borda Count System are used arithmetic to calculate winners based on their ranking. Mathematics assure that the most supported candidate wins, not that one who get most first choice votes.
 - **Probability and Statistical Analysis:** Using probability election result can be predicted which handle uncertainty. Statistical analysis like polling data, historical trends, voter turnout helps to predict the result.

Applications of Mathematics in the Electoral System:



Role of Mathematics in the Pre and Post Elections:

Effectiveness:



Mathematics makes election system more fair and transparent. It helps in several ways:

- Improving Fairness: There are various mathematical models like proportional representation formulae, ranked choice methods that reduce the chance of unfair outcomes.
- **Predicting Outcomes:** Probabilistic and statistical methods can help political analysts, parties and the public to understand possible outcomes. Polls, historical data and demographic data are the main models of predicting Outcomes.
- **Designing Voting Methods:** Various voting methods like ranked choice or mixed systems can be tested mathematically for fairness, transparent and voter satisfaction.
- **Decision-Making and Policy Planning:** Governments and policymakers can use mathematical models to design better electoral rules, or plan strategically.

Shortcomings:

- **Simplifying complex behaviour:** As voter behaviour is affected by culture, emotions, and social factors, so mathematical methods cannot fully connected with human psychology.
- **Dependence on Data Quality:** As mathematical models depends on polls, surveys and historical data, so inaccurate data can be give on to a wrong prediction.
- **Complexity:** Simulations or game theory models are the advanced mathematical models that can be too complicated for practical use.
- **Predictive Limitations:** Some offensive behaviour, sudden voter mobilization can make predictions inaccurate.

Conclusion:

- 176 In conclusion, mathematics plays a vital role in electoral system by making election fair and
- transparent. Using Mathematical models we can design various voting systems, analyze
- voting pattern, predict the result and also can study about gerrymandering. Probability,
- statistics, game theory, graph theory are the branches of mathematics. With the help of these
- election system can be more fair and transparent.

Reference:

- 182 1. Balinski, M. L., & Young, H. P. (2001). Fair Representation: Meeting the Ideal of One Man,
- One Vote. Washington, DC: Brookings Institution Press.

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- 2. Blais, A. (2000). To Vote or Not to Vote: The Merits and Limits of Rational Choice Theory. Pittsburgh: University of Pittsburgh Press. 3. Brams, S. J.,&Taylor, A. D. (1996). Fair Division: From Cake-Cutting to Dispute Resolution. Cambridge: Cambridge University Press. 4. Gini, C. (1936). On the Measurement of Concentration and Inequality. Journal of the Royal Statistical Society, 99(3), 456–473. 5. Golosov, G. V. (2010). The Effective Number of Parties: A New Approach. Party Politics, 16(2), 171–192. 6. Johnston, R. J., Rossiter, D. J., & Pattie, C. J. (2006). Disproportionality and Bias in the Results of the 2005 General Election in Great Britain: Evaluating the Electoral System's Impact. Journal of Elections, Public Opinion and Parties, 16(1), 37–54. 7. Lijphart, A. (1999). Patterns of Democracy: Government Forms and Performance in Thirty-Six Countries. New Haven: Yale University Press. 8. Monroe, B. L. (1995). Fully Proportional Representation. American Political Science Review, 89(4), 925–940.
- 9. Norris, P. (2004). Electoral Engineering: Voting Rules and Political Behavior. Cambridge:
 Cambridge University Press.

218	
219 220	10. Rae, D. W. (1971). The Political Consequences of Electoral Laws. New Haven: Yale University Press.
221	
222	
223 224	11. Riker, W. H. (1982). Liberalism Against Populism: A Confrontation Between the Theory of Democracy and the Theory of Social Choice. San Francisco: W. H. Freeman.
225	
226	
227 228	12. Sartori, G. (1997). Comparative Constitutional Engineering: An Inquiry into Structures, Incentives and Outcomes. New York: NYU Press.
229	
230	
231 232	13. Shugart, M. S., & Wattenberg, M. P. (Eds.). (2001). Mixed-Member Electoral Systems: The Best of Both Worlds? Oxford: Oxford University Press.
233	
234	
235236	14. Taagepera, R., & Shugart, M. S. (1989). Seats and Votes: The Effects and Determinants of Electoral Systems. New Haven: Yale University Press.
237	
238	
239 240	15. Tideman, T. N. (2006). Collective Decisions and Voting: The Potential for Public Choice. Aldershot: Ashgate.
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