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RESEARCH ARTICLE

Energy Dependence Parameter as Mean Charged Multiplicity for Proton-Proton Interactions

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Abstract

The theoretical study of energy dependence of charged multiplicity could discriminate among the different theoretical models of particle production. In the present work, an attempt has been made to analyse the data on mean charged multiplicity in Hadron-Hadron interactions and also to modify the earlier parameterization with modified values of different parameters on the basis of some unambiguous phenomenon. The mean charged multiplicity has been calculated at different energies, ranging between 1.0 GeV to 1500 GeV for proton-proton interactions and the results are compared with experimental data as well as, with other theoretical results. Proposed parameterization is found to be capable of predicting the entire data, even at threshold energy.

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INTRODUCTION

During last several years, the Hadron-Hadron [1-5] and Hadron-Nucleus [6-10] interactions have been attracting considerable attention of high energy physicists. In the field of high energy physics, the mean charged Hadron multiplicity has been an important phenomenological parameter to study the properties of particle production. During last few decades, a considerable amount of the data on mean charged multiplicities has become available at high energies [11-18]. And the theoretical studies of energy dependence of charged multiplicity could discriminate among the different theoretical models of particle production [12-16].

The concept of multiplicity arises from the production in the inelastic events of interaction process. To predict the experimental data, several authors [19-22] have proposed different parameterizations and fittings of charged multiplicity as a function of centre of mass (c.m.) energy (\sqrt{s}). At high energies, the concept of secondary production reveals, that the number of relativistic charged particles, produced in any collision, increases as the incoming beam energy increases. A comparative slow increase in the charged multiplicity is also found, with the increase in the size of target nucleus. Such an increase in the multiplicity occurs only in the central region of the rapidity space of particle production and it is believed that quarks and gluons should play an important role in the process of particle production in the central region. The available data [11-13, 16] on multiplicities as a function of energy indicates that at high energies, the mean charged multiplicity $\langle n_{ch} \rangle$ in different Hadron-Hadron collisions (p-p, p- \bar{p} , π^+p etc.) tends to become independent of the type and the charge of the incident and target particles. This behavior of $\langle n_{ch} \rangle$ seems to be valid also at lower energies and also for photon-Hadron [17-19], lepton-Hadron [22-24] and lepton-lepton [19-21] collisions. Thus it would seem that the entire mean charged multiplicities will follow a universal curve.

Different authors have given different fittings [11-14, 22] for multiplicity, produced in Hadron-Hadron collisions. But there is a large discrepancy in different fittings. In the present work, an attempt has been made to analyse the experimental observations on mean charged multiplicity at various energies for Hadron-Hadron interactions. Different parameterizations proposed by different authors, have been studied and an efforts is done to modify the earlier parameterization [12-16, 22]. The values of different parameters have been fixed on the basis of some unambiguous phenomenon. The present parameterization has been used to calculate the mean charged multiplicity as a function of incident c.m. energy for proton-proton.

Earlier Parameterization

To predict the experimental data, different authors [11-16, 21-22, 29] have given different fittings, depending upon the c.m. (\sqrt{s}). In experimental studies of particle production in Hadron-Hadron interactions, some following general features have been considered,

- Limited transverse momentum of the secondaries.
- Leading particle effect i.e. the incident Hadron retains on an average half of its initial energy.
- Slow increase in the multiplicities of produces particles, consisting mainly of pions, with increase in energy and these are on an average 2/3 charged and 1/3 neutral particles in the final state.
- The multiplicity depends on the centre of mass energy.

Some models predict, at asymptotic energies, an energy dependence of mean charged multiplicity $\langle n_{ch} \rangle$ of the 'ln s' type and the others, a dependence faster than 'ln s' or power dependence on 'ln s' and 's', also more specifically,

- The Cheng-wu model [22] gives $\langle n_{ch} \rangle \sim S^B$ i.e. $\langle n_{ch} \rangle = A S^B$
Where $A = 1.42 \pm 0.01$, $B = 0.28 \pm 0.01$
- The multiperipheral model [21] and the Mueller-Ragge analysis predict $\langle n_{ch} \rangle \sim \ln s$ i.e. $\langle n_{ch} \rangle = A + B \ln s$; $A = -0.67 \pm .04$, $B = 1.32 \pm 0.01$
- The Thermodynamical model [12, 16] predict an energy dependent multiplicity faster than 'ln s' i.e. $\langle n_{ch} \rangle = A + B (\ln s)^2$; $A = 1.73 \pm 0.02$, $B = 0.17 \pm 0.01$ and $\langle n_{ch} \rangle = A + B + C (\ln s)^2$; $A = 1.73 \pm 0.02$, $B = 0.17 \pm 0.01$ and $C = 0.13 \pm 0.01$
- Fermi's old statistical model [25] and Belenjki and Landau's Hydrodynamical model [22] predict that $\langle n_{ch} \rangle = A + B \ln s + C S^{-1/2}$; with $A = -4.55 \pm 0.20$, $B = 1.99 \pm 0.04$ and $C = 8.16 \pm 0.42$

Present Parameterization

An analysis of the available data on mean charged multiplicity has been considered, in the present work, with a view to finding whether,

- The mean charged multiplicity $\langle n_{ch} \rangle$ data can be parameterized low as well as at high values of the energy, by the same parameterization.
- Each term may explain the related physical concept or phenomena of interaction process. For it, we have considered that all the parameters A, B and C should be energy dependent so that they may be consistent with the associated phenomenology.
- Any regular feature of mean charged multiplicity $\langle n_{ch} \rangle$ as a function of c.m. energy may be inferred.

In the present work, an attempt is made to modify the earlier parameterization, $\{\langle n_{ch} \rangle = A + B \ln s + C (\ln s)^2\}$ on the basis of some phenomenological concepts. The various terms of the present parameterization have their own identity and may express the contribution of particular type of interaction process. To predict the experimental data, the value of the parameter A is considered to be constant, but the values of the parameters B and C are considered to be variable, depending upon some other factors, based on the concerned interaction process. The present parameterization for mean charged multiplicity in Proton-Proton interaction has the following form,

$$\langle n_{ch} \rangle_{hh} = A + B \ln \sqrt{S_A} + C (\ln \sqrt{S_A})^2 \quad \text{-----(1)}$$

Here $\sqrt{S_A}$ represents the available centre of mass energy (i.e. $\sqrt{S_A} = \sqrt{S} - m_p - m_t$), \sqrt{S} the centre of mass energy, m_p the mass of projectile and m_t the mass of target nucleus. The values of the parameters A, B and C are considered on the basis of interaction process. The different terms of the above equation signifies their individual contribution, viz. the first term {i.e. A} gives the mean charged multiplicity $\{\langle n_{ch} \rangle\}$, even at threshold energy of particle production in hadronic interaction {i.e. 1GeV}. Since the particle production in any interaction is the result of the formation of quark-gluon plasma and this state is found to be near 1 GeV interaction energy, therefore the minimum charged multiplicity, in charged hadronic interactions may be two.

The second term {i.e. $B \ln \sqrt{S_A}$ } represents the contribution due to direct interaction process. The value of parameter B is considered, in this work, to be dependent on the ratio ρ of the real to the imaginary part of the coulomb amplitude, which is related with the total and scattering cross-section as $\rho = \frac{\sigma_{tot.}}{\sigma_{el.}}$ and is energy dependent. The parameter B is related with ρ by the relation $B = (1 + \rho)$. The various values of ρ at different c.m. energies may be obtained by its above relation with $\sigma_{tot.}$ and $\sigma_{el.}$ [26-27], as shown in Fig.2 for proton-proton and proton-antiproton interactions. And finally the third term {i.e. $C (\ln \sqrt{S_A})^2$ } gives the contribution due to fire-ball formalism in the interaction process. The value of parameter C is considered, in the present work, to be dependent on the absorption coefficient α_s as $C = \frac{4\alpha_s}{3\pi} = 0.4246 \alpha_s$ [25] where $\pi = 3.14$ also $\alpha_s = (1 - \alpha)$ where α is inelastic coefficient and has different values at different incident energies. The different parameters are supposed to have their origins from Quantum Chromo dynamics (QCD). For the various values of α at different c.m. energies, we have used our earlier work [28] to obtain the different values of the parameter C.

Result and Discussion

The mean charged multiplicities $\langle n_{ch} \rangle_{pp}$ for proton-proton interactions is calculated in this work, at different energies, using present parameterization (eq. 1). Various values of $\langle n_{ch} \rangle_{pp}$ at different c.m. energy are given in the Table along with the corresponding experimental data. As a function of incident energy for proton-proton interactions, the available energy has been calculated by the subtraction of rest mass energy of the projectile and target protons {i.e. $\sqrt{S_A} = \sqrt{S} - 1.862$ } GeV. These mean charged multiplicities are plotted in the Fig.1. The energy range, to calculate $\langle n_{ch} \rangle$ for proton-proton interaction, is considered between 1.0 GeV to 1500 GeV. In the case of proton-proton interactions, a slow increase in $\langle n_{ch} \rangle_{pp}$ are found, as the incident energy increases. The results of the present parameterization are well in consistent with the experimental data. A slight deviation of experimental data from the proposed fitting is due to some experimental errors. At very low energies viz. $\sqrt{S} = 5.0$ GeV the value of $\langle n_{ch} \rangle$ in proton-proton interaction is found to be 3.04 and this difference increases continuously with the increase in the c.m. energy. At high energies viz. $\sqrt{S} = 1500$ GeV, the values of $\langle n_{ch} \rangle$ for proton-proton is found to be 12.08. In the present work, we have proposed the values of the parameters B and C, to be energy dependent. The different values of B are calculated by the relation ($B = 1 + \rho$) at different energies and are presented in the Table for proton-proton. Also the different values of C are calculated by the relation ($C = \frac{4\alpha_s}{3\pi}$) at different values of \sqrt{S} , and are presented in the respective tables for proton-proton interactions. The variation of the parameter B, with c.m. energy \sqrt{S} , for proton-proton is shown in Fig.3. Since the second term of the present parameterization gives the inelastic contribution and thus the parameter B is related to the ratio ρ of the real to the imaginary part of the scattering amplitude, therefore the values of B are found to be increasing slowly in the case of proton-antiproton interactions in comparison to that in the case of proton-proton interactions. The variations in B, in both the cases, may also be inferred from the variation in ρ with c.m. energy [26-27] as given in Fig.2. The variation of the parameter C with \sqrt{S} for proton-proton is shown in Fig.4. Since the third term gives the contribution due to fireball formalism in the interaction process and thus the parameter C is related to the running coupling constant (absorption coefficient) α_s , therefore the value of C is found to be decreasing regularly. C has less value in the case of proton-proton interaction for each value of energy. The variation in parameter C in the case of proton-proton may also be inferred from the variation in α_s [25].

Table: Mean Charged Multiplicity $\langle n_{ch} \rangle_{pp}$ at different c.m. energies in the proton-proton interactions. Here $A = 2$, B and C are calculated as a function of c.m. energy.

C.M. Energy (\sqrt{S}) GeV	Available C.M. Energy ($\sqrt{S_A} = \sqrt{S} - 1.86$) GeV	Parameter (B)	Parameter (C)	$\langle n_{ch} \rangle_{pp}$ (Present Work)	$\langle n_{ch} \rangle_{pp}$ (Experimental)
2.0	0.14	0.73	0.17	1.22	--
3.0	1.14	0.74	0.16	2.09	--
4.0	2.14	0.74	0.16	2.65	--
4.95	3.09	0.75	0.15	3.04	3.24 \pm 0.03

10.25	8.39	0.83	0.14	4.40	4.10 ±0.04
11.70	9.84	0.86	0.13	4.65	4.22 ±0.04
13.50	11.64	0.88	0.11	4.88	4.41 ±0.04
25.0	23.14	0.97	0.08	5.84	5.35 ±0.11
33.95	32.09	1.00	0.07	6.31	5.89 ±0.07
50.0	48.14	1.04	0.06	6.93	6.36 ±0.06
100.0	98.14	1.09	0.05	8.05	7.64 ±0.17
150.0	148.14	1.12	0.05	8.85	8.86 ±0.16
500.0	498.14	1.14	0.04	10.62	10.60 ± 0.60
1000.0	998.14	1.15	0.04	11.84	--
1500.0	1498.14	1.16	0.03	12.08	12.60 ± 0.70

Fig. 1 Variation of mean charged multiplicity ($\langle n_{ch} \rangle_{pp}$) as a function of available c.m. energy ($\sqrt{S_A}$). The curve shows the present work. The experimental data has been taken from ref. [11, 13, 18, and 29]

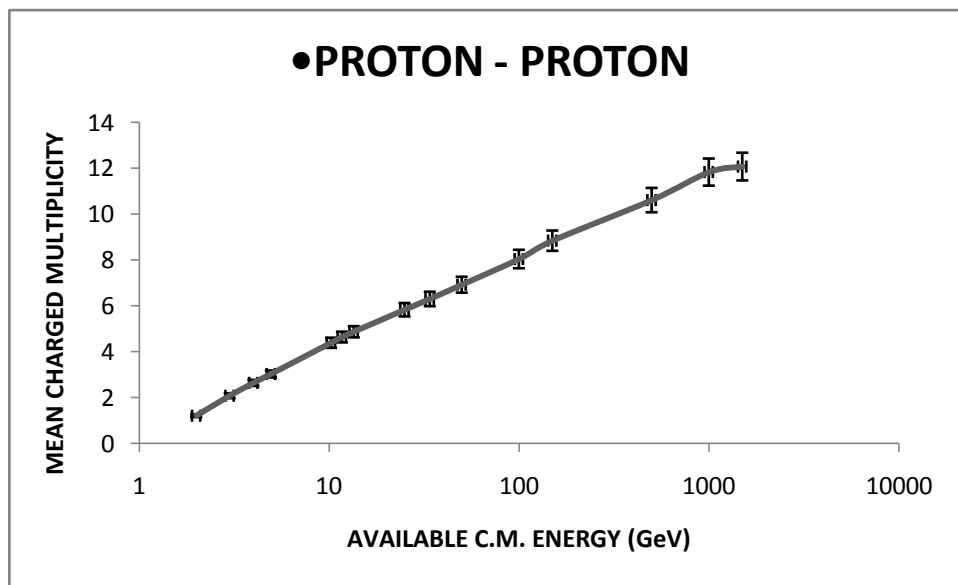
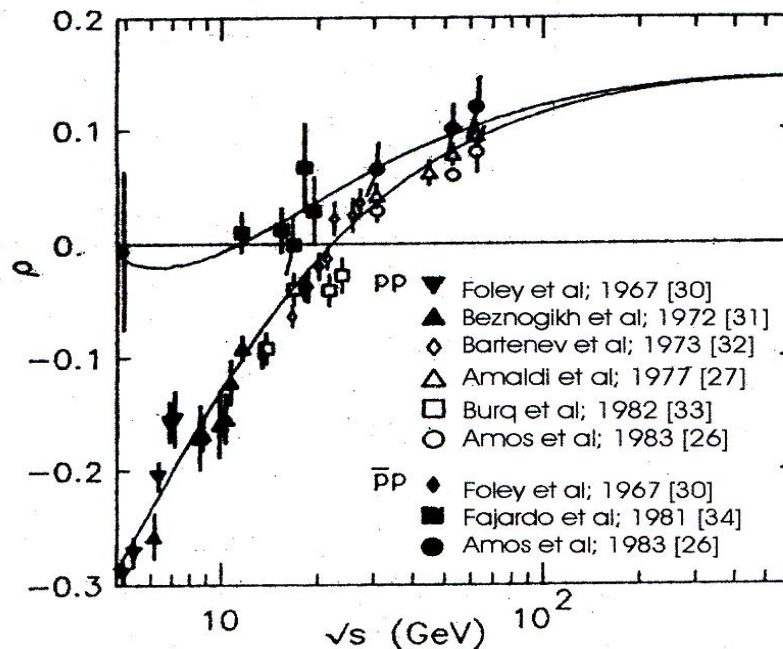


Fig. 2 The ratio ρ of real to imaginary part of the scattering amplitude for p-p and p- \bar{p} interactions as a function of c.m. energy (\sqrt{s}) [26-27]

Fig. 3 Variation of parameter B for proton-proton interactions as a function of available c.m. energy ($\sqrt{S_A}$) GeV.



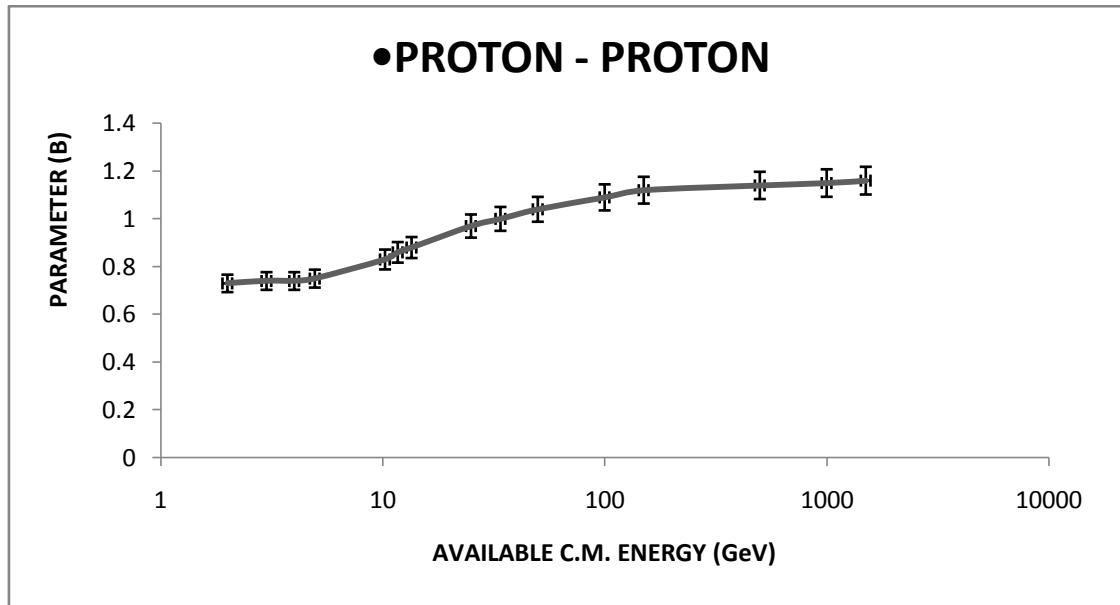
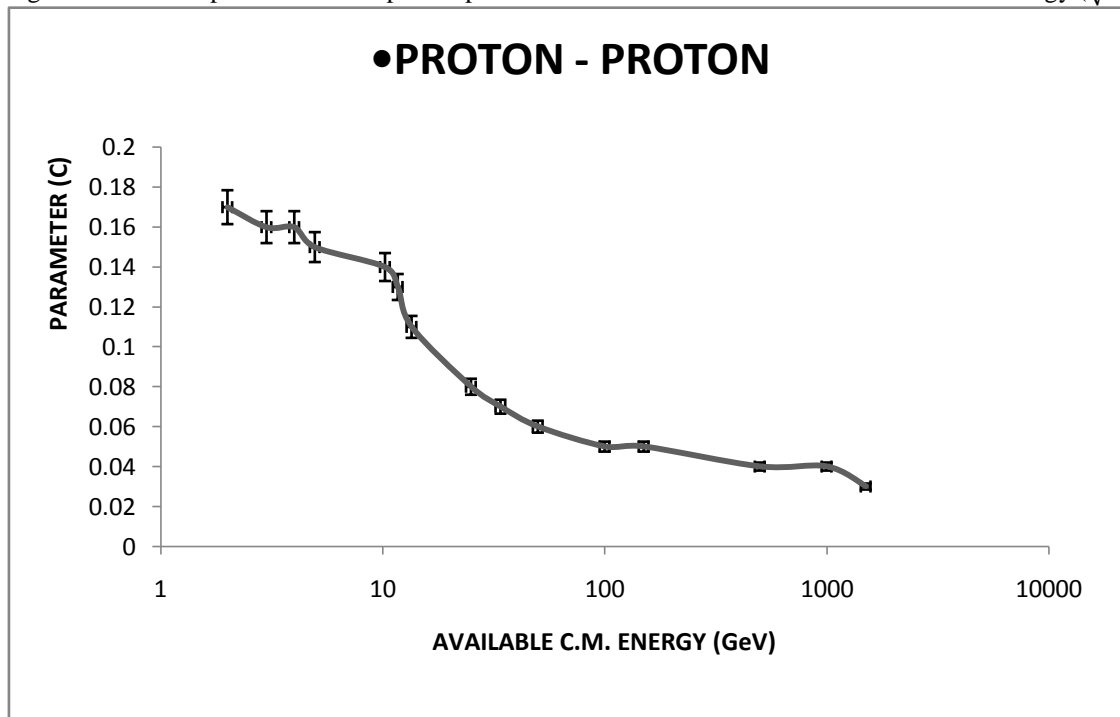


Fig. 4 Variation of parameter C for proton-proton interactions as a function of c.m. available energy ($\sqrt{s_A}$) GeV.



Conclusions

- 1) The present parameterization of mean charged multiplicity $\langle n_{ch} \rangle$ in Hadron-Hadron interactions provides simple and unambiguous results, which are in well consistent with experimental data for the entire range of incident energy.
- 2) The present parameterization is capable of explaining the mean charged multiplicity even at threshold c.m. energy (i.e. 1.0 GeV). It may be 2, one for projectile Hadron and one for target Hadron.

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